



OPERATIONAL RESEARCH

**(CRITICAL PATH METHOD AND
PROJECT EVALUATION REVIEW
TECHNIQUES)**

Network Analysis

- Network analysis is a universal term provided to some particular techniques utilized for the planning, management and control of projects.
 - Definition of a project (from the [Project Management Institute](#)) is:
 - **A project is a temporary endeavour undertaken to create a "unique" product or service.**
 - This definition serves to underline certain elementary characteristics of a project.
 - it is momentary - it has a starting point and a finish point
 - it is therefore "peculiar"

Network Analysis

- Generally, all projects can be divided into:
 - separate *activities* (tasks/jobs) - where each activity has a related lifetime or *completion time* (i.e. the time from the start of the activity to its finish)
 - *precedence relationships* - which manage the order in which we may execute the activities, e.g. in a project concerned with building a house the activity "erect all four walls" must be finished before the activity "put roof on" can start

** The difficulty is to bring all these activities together in a logical manner to complete the project.

Network Analysis

- 2 distinct techniques for Network Analysis originated independently in the late 1950's - these were:
 - PERT (for Program Evaluation and Review Technique); and
 - CPM (for Critical Path Management).
- Network analysis is an essential technique in **PROJECT MANAGEMENT**. It permits us to adopt a *systematic quantitative structured approach* to the challenge of handling a project towards fruitful achievement. Additionally, it has a graphical representation, allowing for better comprehension and use by those who are technically less knowledgeable about it.

Critical Path Activity (CPA)

- It is a mechanism used to plan activities so that a job can be executed in the most efficient way, thus taking minimum time possible.
- It divides a job into multiple tasks and scrutinize the dependency of them
 - ❖ Example: List the activities that must be completed in order to make a cup of tea
- It is widely used in the Manufacturing and Construction Sector

Parts of the Network

- A network consists of 2 things:

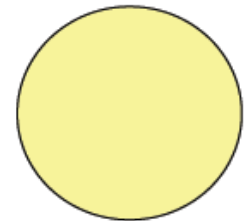
- An **ACTIVITY**

- This requires time and/or resources
- They are drawn as **ARROWS** from left to right
- The length of the arrow is **NOT** important



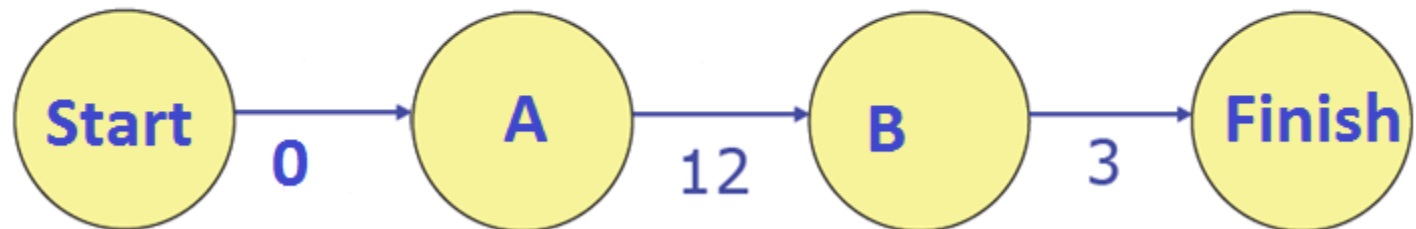
- A **Node**

- These represent the start and the end of an activity
- They are represented by **CIRCLES**
- Every network **MUST** start and end with a node



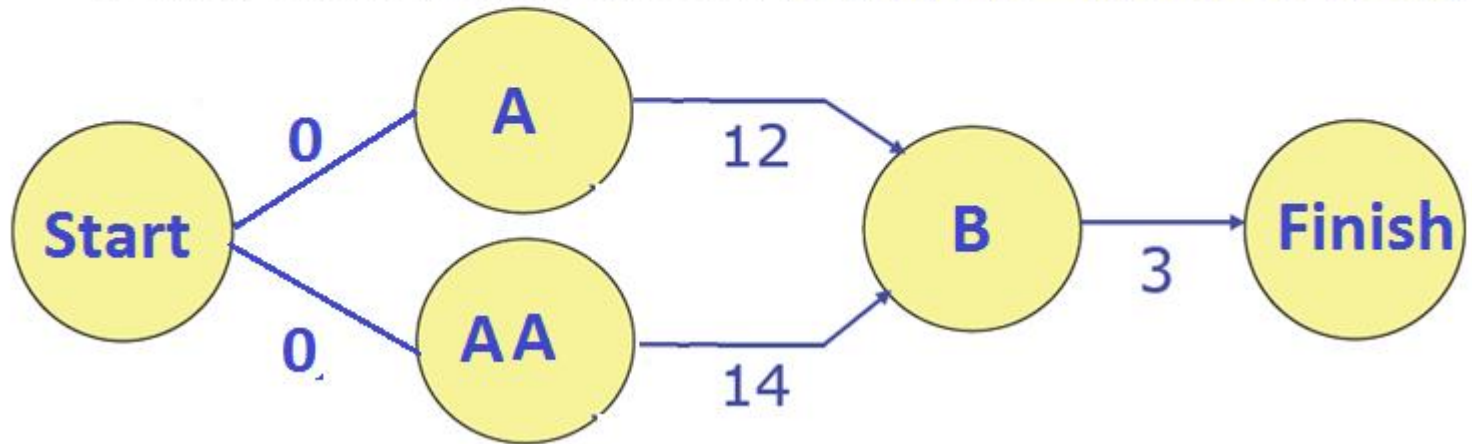
A Simple Network Diagram

- A business wishes to build a new factory
- Before it can do so it needs to:
 - Buy the land (Activity A – will take 12 weeks)
 - Draw up Plans (Activity B – will take 3 weeks)
- A simple network may be drawn to illustrate this scenario:



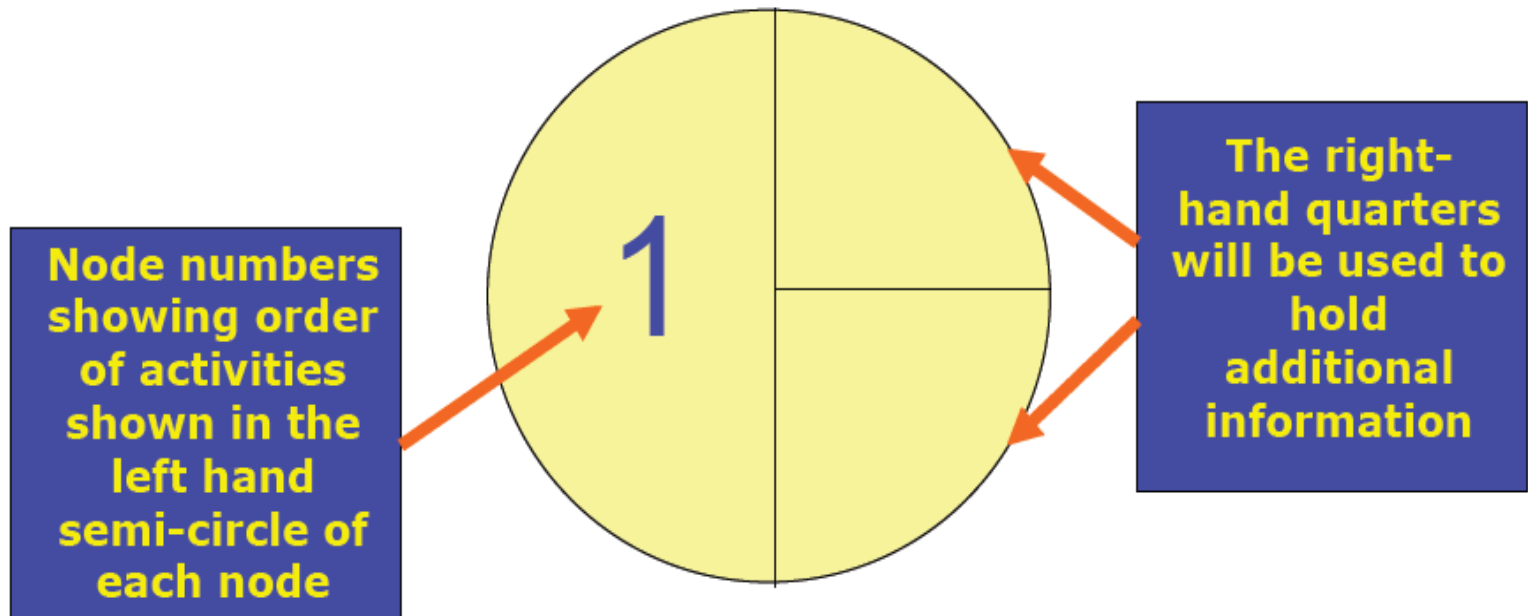
Illustrating Simultaneous Activities

- Of course in reality some activities can be carried out simultaneously
- Using the previous example:
 - Assume that whilst in the process of buying the land the firm wants to apply for planning permission (Activity AA – will take 14 weeks)



Developing the network

- There are a number of problems with our previous example:
 - There is no way of identifying the nodes
 - It doesn't help us identify the crucial activities
- In order to do this the nodes can be developed in order to show more information:



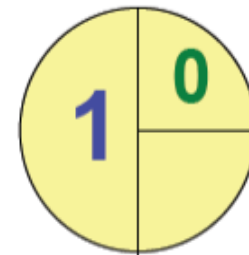
Calculating the earliest start time

- The main reason for drawing a network is to identify the **CRITICAL** activities
- To do this we must calculate the earliest time at which any given activity can start
 - This is called the **Earliest Start Time (EST)** of the activity
- It is calculated using the following formula:

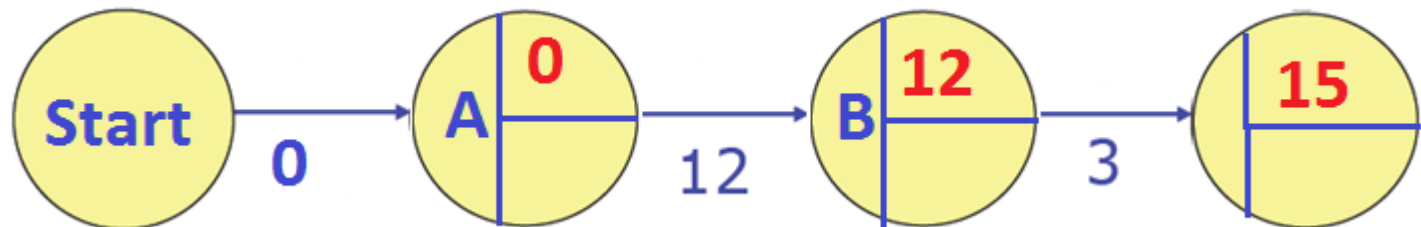
$$\text{EST} = \text{EST of Previous activity} + \text{Duration of previous activity}$$

Calculating the earliest start time

- This information is then placed in the top right-hand quarter of the node
- The first node will **ALWAYS** have an EST of zero
- Using our first simple example, the EST for each activity would be calculated as follows:

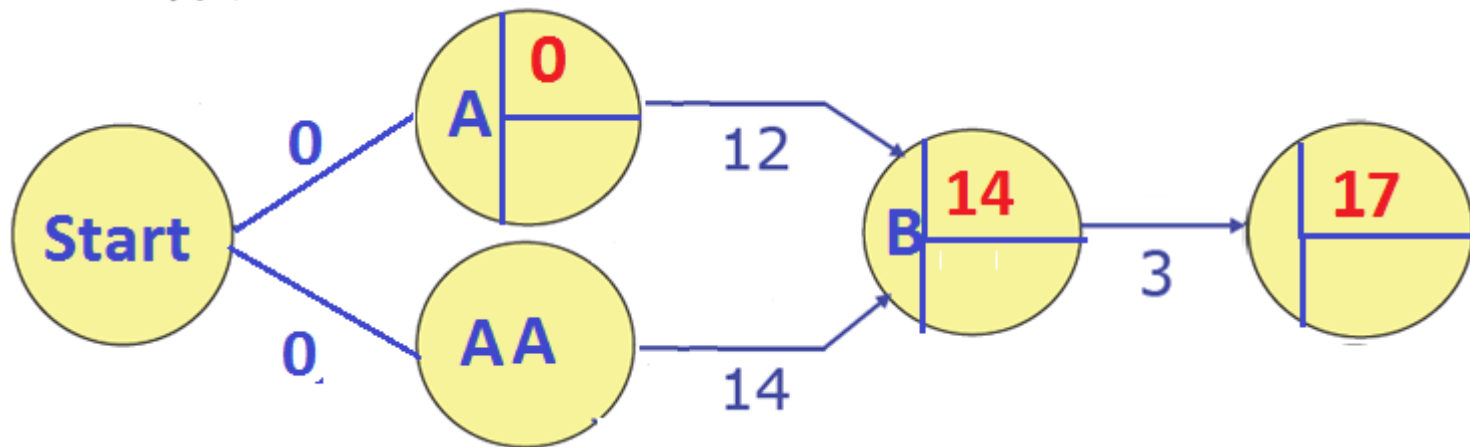


EST goes in top right-hand quarter of the node



The EST & Simultaneous Activities

- When there are simultaneous activities there may be more than one value for the EST



- Since Activity B is **DEPENDENT** on both Activities A and AA, it cannot start until both are complete
- So we must take the **HIGHEST** figure
- This means that the EST is 14 weeks

Recap of Earliest Start Time

- The EST of the first activity is always zero
- Calculate the EST by working left to right across a network
- It is calculated using the following formula:

$$\text{EST} = \text{EST of Previous activity} + \text{Duration of previous activity}$$

- When there are 2 simultaneous activities the **HIGHEST** figure is used as the EST

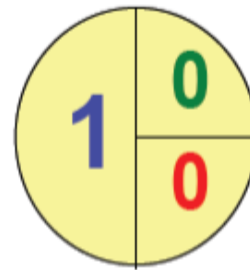
Calculating Latest Finish Time

- There is one final piece of information needed to complete our network diagram
- To identify the **CRITICAL** activities we must also know the latest time at which any given activity must end
 - This is called the **Latest Finishing Time (LFT)** of the activity
- It is calculated by working **BACKWARDS** across the network using the following formula:

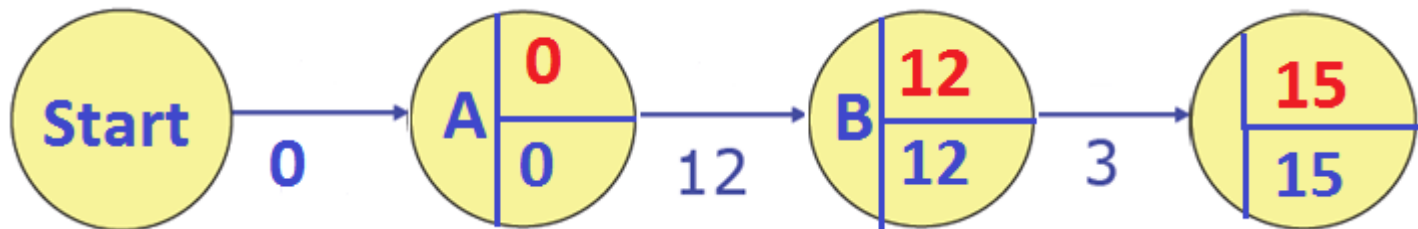
$$\text{LFT} = \text{LFT at end of following activity} - \text{Duration of following activity}$$

Calculating Latest Finish Time

- This information is then placed in the bottom right-hand quarter of the node
- The first node will **ALWAYS** have an LFT of zero
- Using our first simple example, the LFT for each activity would be calculated as follows:



LFT goes in bottom right-hand quarter of node

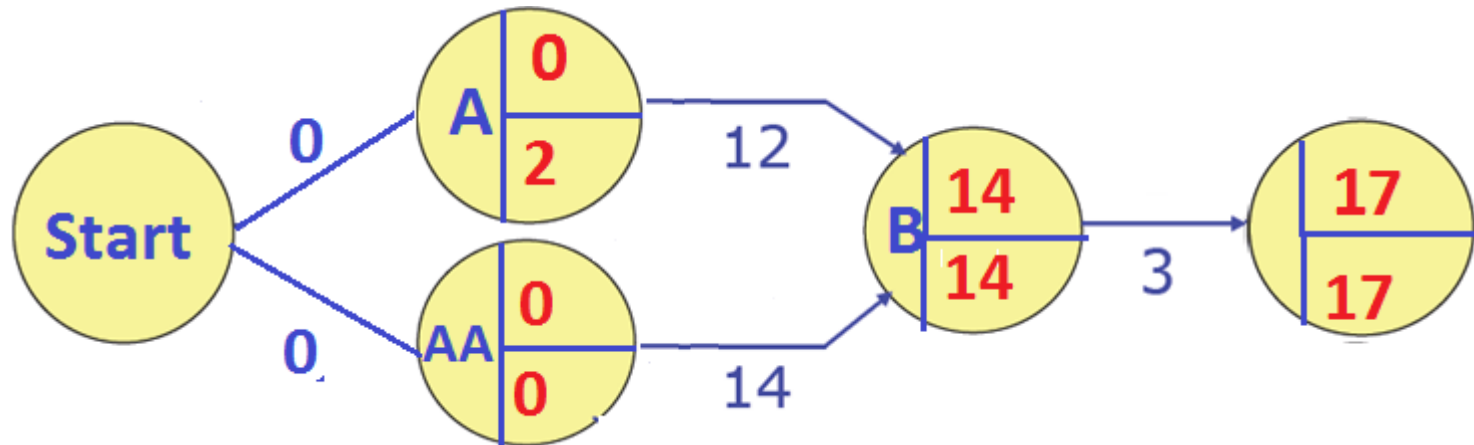


Since the earliest time this project can be finished is 15 weeks then this is also the latest we would like to finish the project. As such:

The EST and LFT of the last node are ALWAYS the same

The LFT & Simultaneous Activities

- When there are simultaneous activities there may be more than one value for the LFT



- If Activity AA starts on week 2 it cannot be completed by week 14
- So we must take the **LOWEST** figure
- This means that the LFT is week 0

Recap of Latest Finish Time

- The LFT of the last activity is always equal to its EST
- The LFT of the first activity is always zero
- Calculate the LFT by working right to left across a network
- It is calculated using the following formula:

$$\text{LFT} = \text{LFT at end of following activity} - \text{Duration of following activity}$$

- When there are 2 simultaneous activities the **LOWEST** figure is used as the LFT

The float

- The vertices with equal EST and LFT define the **critical path**.
- Another way of identifying the critical path is to define the

$$\text{Float time} = \text{LFT} - \text{EST}$$

Calculating the Float

Activity	EST	LFT	Float
A	0	2	2
AA	0	0	0
B	14	14	0

What does this mean?

- This data tells us:
 - That Activity A can be delayed 2 weeks without delaying Activity B
 - That Activity AA is **CRITICAL** – any delay will hold up the project
 - That Activity B is **CRITICAL** – any delay will hold up the project

Advantages of CPA

- It mandates considerate groundwork (planning) so that the project / activity can be conducted efficiently
- Enhances efficiency and cash flow, for e.g. materials will be ordered only upon the necessity
- Should any issue arise, the discrepancies that can be easily identified, hence allowing room for effective decision-making

Disadvantages of CPA

- Graphical representations can be disruptive, even if there is a software to assist with the production of networks
- The plan will function properly with the consultation of relevant staff, e.g, realistic timeframes
- In order to visually demonstrate the chronology of activities, Gantt charts are recommended.